

ICEN Extension to SENKIN Code

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This document describes the zero-dimensional internal combustion engine model used in the ICEN (Internal Combustion Engine) extension to SENKIN^[1] code in Chemkin-II^[2] based on Heywood.^[3]

Although the model and the input parameters were intended to be compatible with the similar extension in Chemkin-3/4, the calculation results are not assured to be the same as them.

1. Nomenclature

The symbols and abbreviation used in this document are listed below.

a	Crank radius	A	Surface area
A_{ch}	Cylinder head surface area	A_p	Piston crown surface area
B	Cylinder bore	c_p	Isobaric specific heat capacity
$C_{p,m}$	Isobaric molar heat capacity	h_c	Heat-transfer coefficient
k	Thermal conductivity	K	Compression ratio
l	Connecting rod length	L	Piston stroke
M_{air}	Molar mass of air	N	Crankshaft rotational speed ($= \omega / 2\pi$)
p	Pressure	Q	Heat
R	connecting rod length / crank radius	R_{gas}	Molar gas constant
s	Crank axis to piston pin distance	\hat{S}_p	Mean piston speed
t	Time	T	Temperature
T_w	Cylinder wall temperature	V_c	Clearance volume
V_d	Displaced cylinder volume	θ	Crank angle ATDC (after TDC)
δ_h	Thickness of thermal boundary layer	ρ	Density
μ	Viscosity	Nu	Nusselt number ($= h_c B / k$)
ω	Crankshaft angular velocity ($= 2\pi N$)	Re	Reynolds number ($= \rho \hat{S}_p B / \mu$)
BDC	Bottom dead center		
Pr	Prandtl number ($= c_p \mu / k$)		
TDC	Top dead center		

2. Piston-Crank Mechanism

From a geometric consideration, as depicted in Fig. 1, the distance, s , between the crank axis and piston pin axis can be written as,

$$s = a \cos \theta + \sqrt{l^2 - a^2 \sin^2 \theta} \quad (1)$$

Since the distance s at the TDC is $s_{TDC} = a + l$, the cylinder volume is,

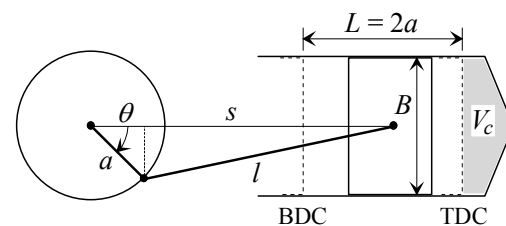


Fig. 1 Schematics of the Piston-Crank Mechanism

^[1] A. E. Lutz, R. J. Kee, and J. A. Miller, SENKIN: *A Fortran Program for Predicting Homogeneous Gas Phase Chemical Kinetics With Sensitivity Analysis*, SAND87-8248-UC-401, Sandia National Laboratories, 1995.

^[2] R. J. Kee, F. M. Rupley, and J. A. Miller, *Chemkin-II: A Fortran Chemical Kinetics Package for the Analysis of Gas-Phase Chemical Kinetics*, SAND89-8009B-UC-706, Sandia National Laboratories, 1995.

^[3] J. B. Heywood, *Internal Combustion Engine Fundamentals*, McGraw-Hill, New York, 1988.

$$V = \frac{\pi B^2}{4}(s_{\text{TDC}} - s) + V_c \quad (2)$$

By using the ratio of connecting rod length to crank radius,

$$R = \frac{l}{a} \quad (3)$$

and the compression ratio,

$$K = \frac{V_d + V_c}{V_c} = \frac{\pi B^2 a}{2V_c} + 1 \quad (4)$$

eq. (2) can be rewritten as,

$$\frac{V}{V_c} = \frac{K-1}{2} \left(1 + R - \cos \theta - \sqrt{R^2 - \sin^2 \theta} \right) + 1 \quad (5)$$

For a constant angular velocity, the time variation is described with,

$$\theta = \theta_0 + \omega t \quad (6)$$

where θ_0 is the crank angle at $t = 0$. Differentiation of eq. (5) with respect to θ gives,

$$\frac{1}{V_c} \frac{dV}{d\theta} = \frac{K-1}{2} \sin \theta \left(1 + \frac{\cos \theta}{\sqrt{R^2 - \sin^2 \theta}} \right) \quad (7)$$

The time derivative of the volume is given by,

$$\frac{dV}{dt} = \omega \frac{dV}{d\theta} \quad (8)$$

Similarly, the cylinder surface area is given by,

$$A = A_{\text{ch}} + A_p + \frac{2V_c(K-1)}{B} \left(1 + R - \cos \theta - \sqrt{R^2 - \sin^2 \theta} \right) \quad (9)$$

For flat-topped piston and cylinder,

$$A_p = \frac{\pi B^2}{4} \quad (10)$$

$$A_{\text{ch}} = \frac{\pi B^2}{4} + \frac{4V_c}{B} \quad (11)$$

The mean piston speed is defined as,

$$\hat{S}_p = 2LN = \frac{8V_c(K-1)}{\pi B^2} N \quad (12)$$

3. Heat Transfer

For a forced-convection condition, the rate of heat-transfer is described by,

$$\frac{dQ}{dt} = h_c A (T - T_w) \quad (1)$$

The heat-transfer coefficient h_c is related to the thermal conductivity k and the thickness of the thermal boundary layer δ_h by a simple boundary layer model,

$$h_c = \frac{k}{\delta_h} \quad (2)$$

Thus the main problem of the forced-convection heat-transfer is in the estimation of δ_h or the Nusselt dimensionless number Nu ,

$$Nu = \frac{B}{\delta_h} = \frac{h_c B}{k} \quad (3)$$

Note that in this document, the *characteristic length* in a dimensionless number is taken to be the cylinder bore B . In many empirical correlations, Nu is written by Reynolds and Prandtl numbers, Re and Pr , respectively, as,

$$Nu = a Re^m Pr^n \quad (4)$$

The Reynolds and Prandtl numbers are defined as,

$$Re = \frac{\rho \hat{S}_p B}{\mu} \quad (5)$$

$$Pr = \frac{c_p \mu}{k} \quad (6)$$

By assuming that the gas property is dominated by that of air, ρ , k , μ , and c_p are approximated as,

$$k \approx k(\text{air}) = 3.50 \times 10^{-4} T^{0.764} [\text{J m}^{-1} \text{s}^{-1} \text{K}^{-1}] \quad (7)$$

$$= 35.0 T^{0.764} [\text{erg cm}^{-1} \text{s}^{-1} \text{K}^{-1}] \quad (7')$$

$$\mu \approx \mu(\text{air}) = 4.41 \times 10^{-7} T^{0.664} [\text{kg m}^{-1} \text{s}^{-1} = \text{Pa s} = \text{N s m}^{-2}] \quad (8)$$

$$= 4.41 \times 10^{-6} T^{0.664} [\text{g cm}^{-1} \text{s}^{-1} = \text{dyn s cm}^{-2}] \quad (8')$$

Widely used Woschni's correlation assumes that $a = 0.035$ and $n = 0$ in eq. (4),

$$Nu = 0.035 Re^m \quad (9)$$

In many cases, the exponent m is chosen to be 0.8.