

Fig. 3.1 Rotational distribution of CN formed via $\text{HCN} + h\nu$ (channel-1)

Rotational sum

$$\rho_{rot-sum} = C_{rot-sum} E^{\frac{n_r+1}{2}} \quad (3.1.4)$$

$$C_{rot-sum} = \frac{\Gamma\left(\frac{n_t}{2}\right) \prod_{i=1}^{m_r} \Gamma\left(\frac{n_{r,i}}{2}\right)}{\Gamma\left(\frac{n_t + n_r}{2}\right)} c_{trans} \prod_{i=1}^{m_r} c_{rot}^{(n_{r,i})} \quad (3.1.5)$$

- for integer n : $\Gamma(n) = (n-1)!$, $\Gamma(1) = \Gamma(2) = 1$
- for half integer n : $\Gamma(1/2) = \pi^{1/2}$, $\Gamma(3/2) = \Gamma(1/2) \times (1/2) = \pi^{1/2} / 2$, ...

product pair	n_r	$C_{rot-sum}$
linear + atom	2	$\frac{\Gamma(1.5)\Gamma(1)}{\Gamma(2.5)} c_{trans} c_{rot}^{2D} = \frac{2}{3} \frac{c_{trans}}{\sigma B}$
non-linear + atom	3	$\frac{\Gamma(1.5)\Gamma(1.5)}{\Gamma(3)} c_{trans} c_{rot}^{3D} = \frac{\pi}{4} \frac{c_{trans}}{\sigma B_{av}^{3/2}}$
linear + linear	$2 + 2 = 4$	$\frac{\Gamma(1.5)\Gamma(1)\Gamma(1)}{\Gamma(3.5)} c_{trans} c_{rot,1}^{2D} c_{rot,2}^{2D} = \frac{4}{15} \frac{c_{trans}}{\sigma_1 B_1 \sigma_2 B_2}$
linear + non-linear	$2 + 3 = 5$	$\frac{\Gamma(1.5)\Gamma(1)\Gamma(1.5)}{\Gamma(4)} c_{trans} c_{rot,1}^{2D} c_{rot,2}^{3D} = \frac{\pi}{12} \frac{c_{trans}}{\sigma_1 B_1 \sigma_2 B_{av,2}^{3/2}}$
non-linear + non-linear	$3 + 3 = 6$	$\frac{\Gamma(1.5)\Gamma(1.5)\Gamma(1.5)}{\Gamma(4.5)} c_{trans} c_{rot,1}^{3D} c_{rot,2}^{3D} = \frac{8\pi}{105} \frac{c_{trans}}{\sigma_1 B_{av,1}^{3/2} \sigma_2 B_{av,2}^{3/2}}$

Vibrational sum

$$\rho_{vib-sum-cl} = \frac{\Gamma(l_r + 1)}{\Gamma(l_r + n_v + 1)} \frac{C_{rot-sum}}{\prod_{i=1}^{n_v} h\nu_i} E_{cl}^{(l_r + n_v)} \quad (3.2.2)$$

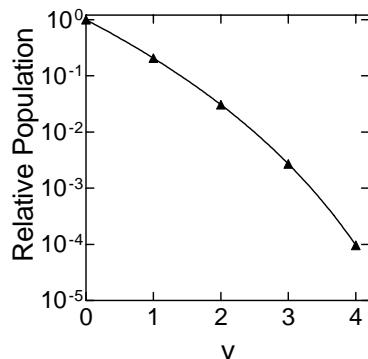


Fig. 3.2 Vibrational distribution of OH formed via $\text{O}({}^1\text{D}) + \text{CH}_4$

Problem-3.4

Calculate the *prior* branching fractions for the reaction of $\text{O}({}^1\text{D})$ with CH_4 ,

$\Delta H^\circ_{0\text{K}} / \text{kJ mol}^{-1}$		
$\text{O}({}^1\text{D}) + \text{CH}_4$	$\rightarrow \text{CH}_3 + \text{OH}$	-182.7
	$\rightarrow \text{CH}_3\text{O} + \text{H}$	-129.1
	$\rightarrow \text{CH}_2\text{OH} + \text{H}$	-173.2
		channel- <i>a</i>
		channel- <i>b</i>
		channel- <i>c</i>

at room temperature (298 K). Two experimental measurements on H-atom reported the sum of branching fractions for channel-*b* and *c* as 14% and 25%. Compare these with the prior branching fractions.

Molecular constants

chemical species	H	OH	CH_3	CH_3O	CH_2OH
mass / amu	1.008	17.003	15.024	31.019	31.019
symmetry	–	$C_{\infty v}$	D_{3h}	C_{3v}	C_1
rot. sym. num. σ	1	1	6	3	1
num. opt. isom. n_{OPT}	1	1	1	1	2
electronic state	$1^2S_{1/2}$	$X^2\Pi$	$\tilde{X}^2\text{A}_2''$	\tilde{X}^2E	\tilde{X}^2A
deg. of electron. state g_e	2	4	2	4	2
rot. deg. of freedom n_r	–	2	3	3	3
rot. consts. / cm^{-1}					
<i>A</i>			(= <i>B</i>)	5.169	6.555
<i>B</i>		18.51	9.578	0.9317	1.0061
<i>C</i>			4.742	(= <i>B</i>)	0.8879
vib. deg. of freedom n_v	–	1	6	9	9
vib. frequencies* / cm^{-1}					
ν_1		3568	3004	2840	3650
ν_2			606	1362	3019
ν_3			3161 (2)	1047	2915
ν_4			1396 (2)	2774 (2)	1459
ν_5				1487 (2)	1334
ν_6				652 (2)	1183
ν_7					1048
ν_8					607
ν_9					420

* Numbers in parentheses are degeneracy of the vibrational modes.

$$1 \text{ cm}^{-1} = 11.96266 \text{ J mol}^{-1}, R = 8.31451 \text{ J K}^{-1} \text{ mol}^{-1}$$